

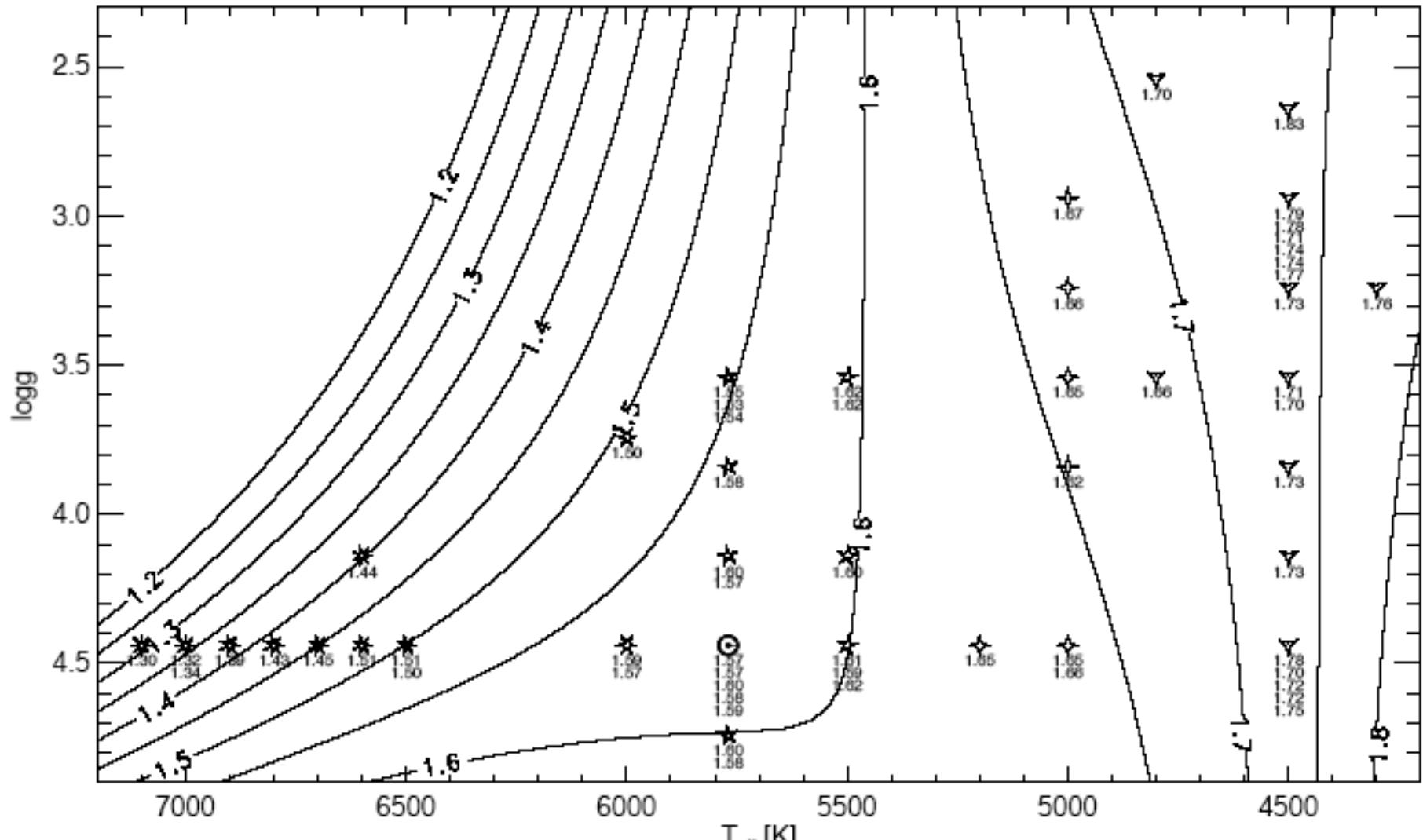
# Convective and non-convective mixing in AGB stars

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Los Alamos National Laboratory  
Theoretical Astrophysics Group

## Variation of mixing length parameter:

Calculated from a grid of RHD convective envelope models for sun-like stars

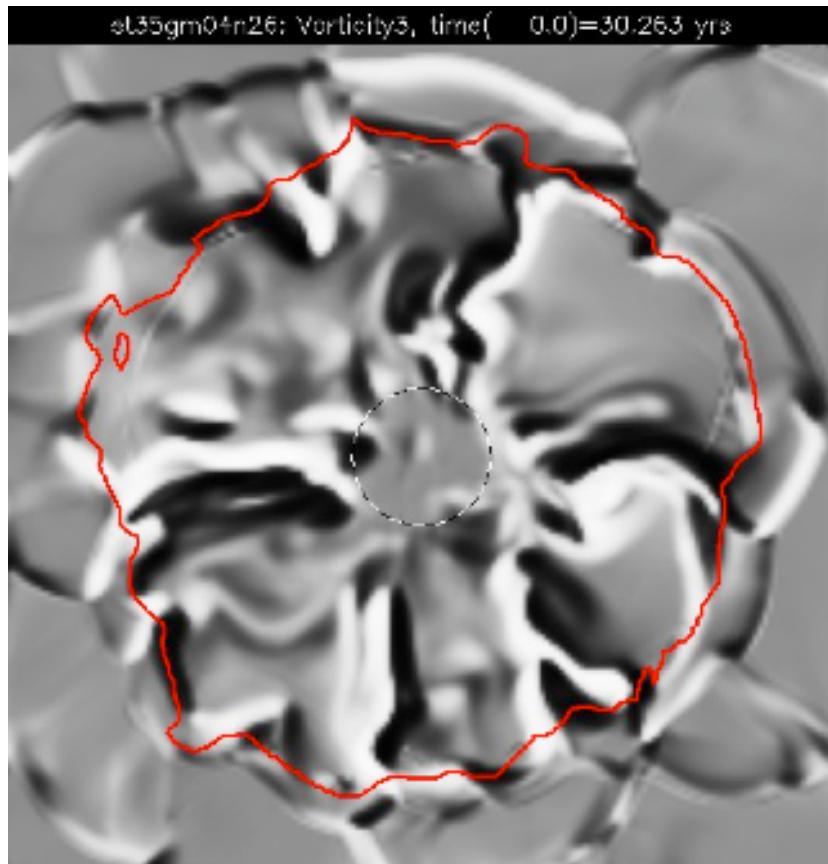


Ludwig et al 1999

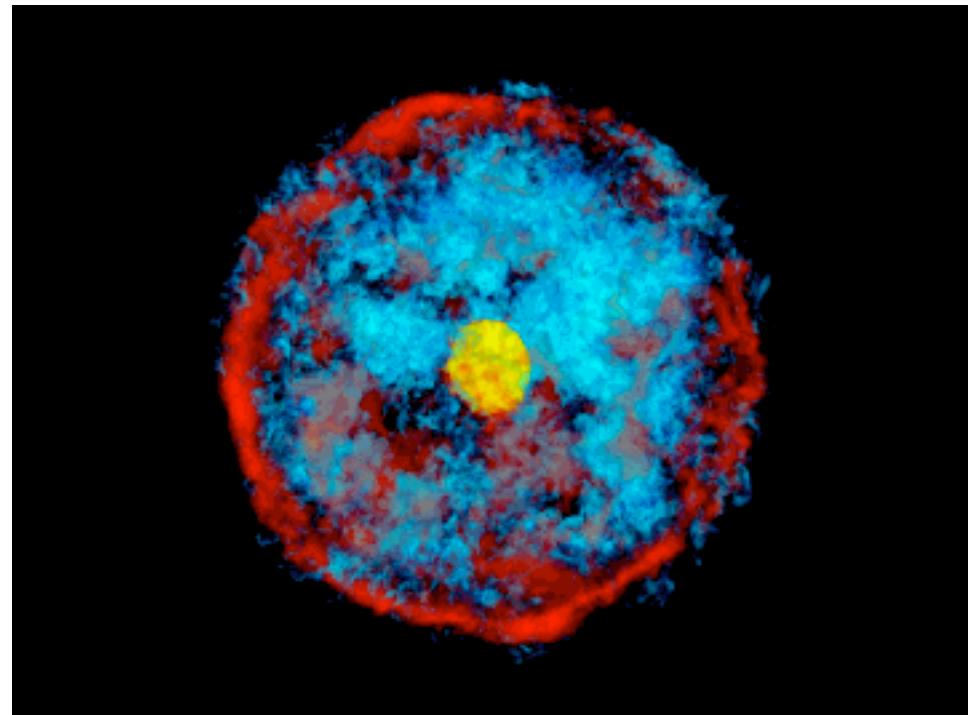
## 3D hydro simulations of AGB convective envelopes

Simulations by Bernd Freytag (left) and Paul Woodward and David Porter (right)

Vorticity:



Temperature fluctuations:



Porter & Woodward 2000, ApJS 127, 159

<http://www.astro.uu.se/~bf>

<http://www.lcse.umn.edu/research/RedGiant>

# Multi-dimensional hydrodynamics simulations of He-shell flash convection

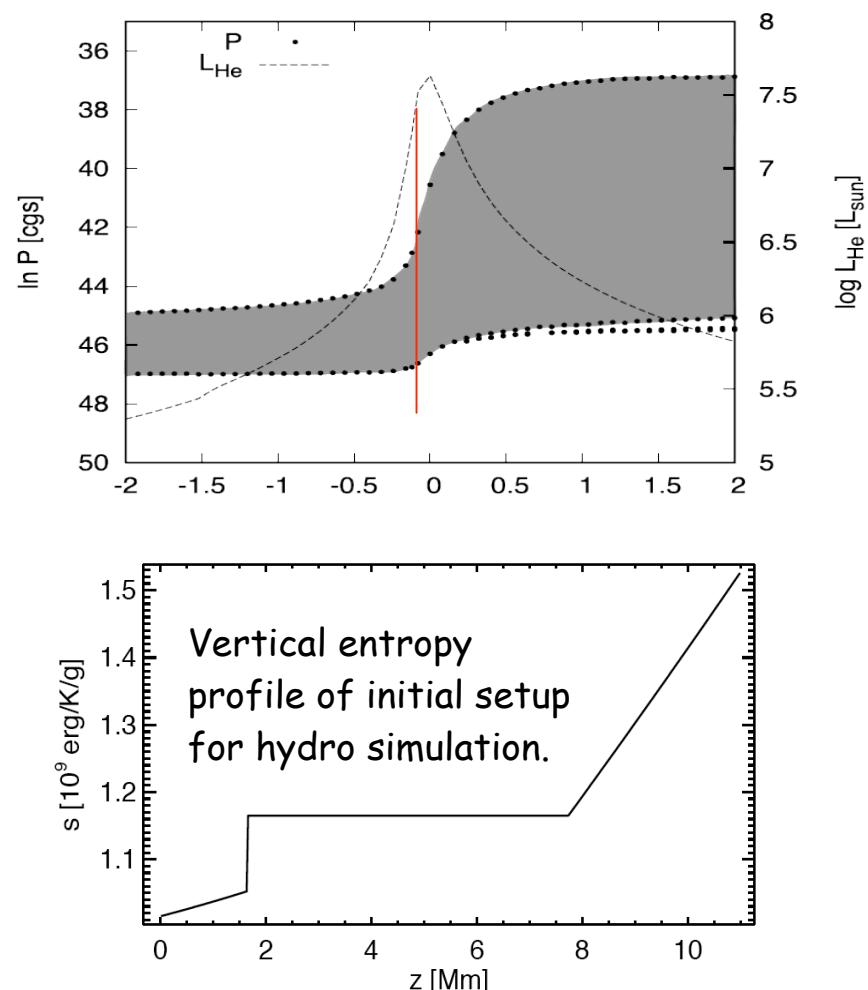
## Goals:

- Topology of He-shell flash convection - how does it look like?
- Velocity distribution for short-lived T-dependent s-process branchings (e.g.  $^{128}\text{I}$ , Reifarth et al. 2004, ApJ)
- Entrainment (mixing across convective boundaries): there is a continuous range from classical overshooting to gravity wave turbulent mixing
- Next step: H-ingestion into He-shell flash (metal poor AGB stars, post-AGB born-again stars)

Collaborators: Bernd Freytag, Robert Hueckstaedt, Frank Timmes  
Herwig et al 2006, ApJ 642, 1057, Freytag et al. 2006, in prep.

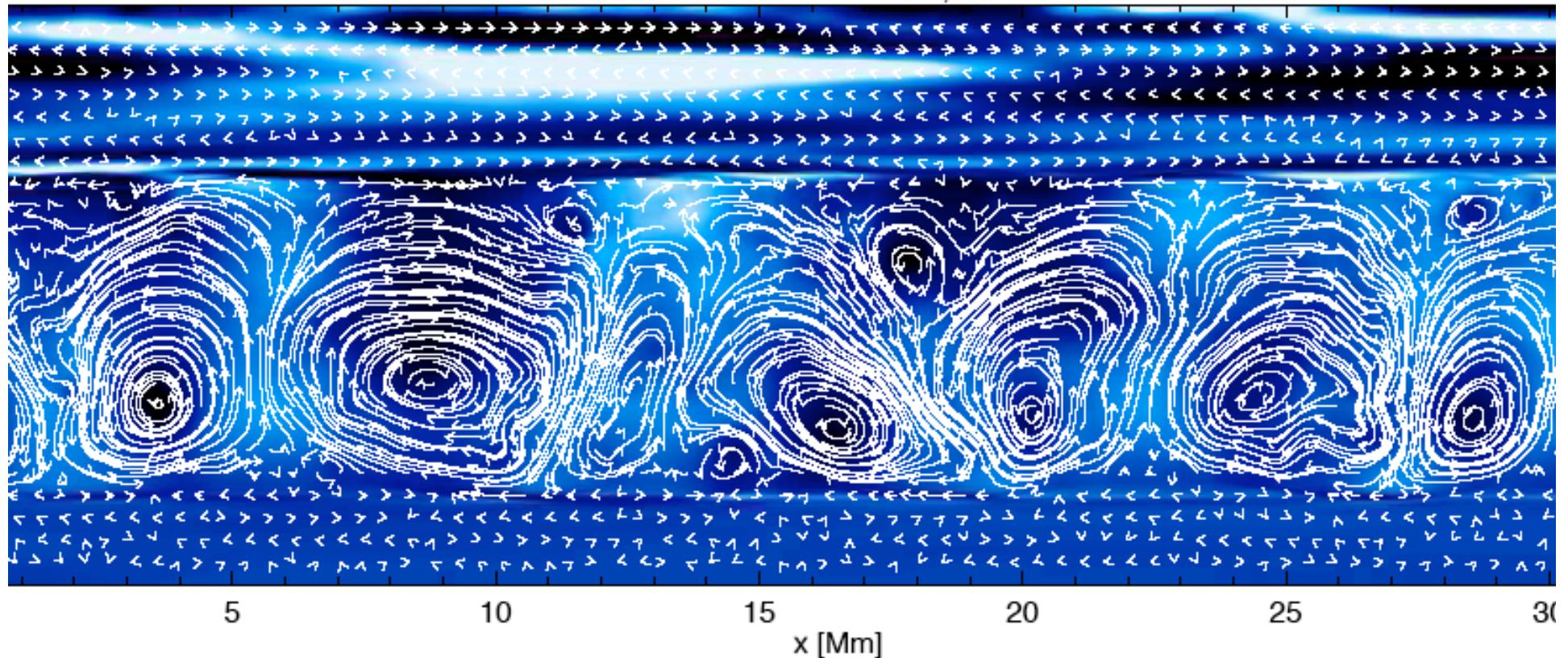
# Setup, code, initial conditions

- 2D and 3D hydrodynamics simulations of a short duration ( $\sim 20\text{ksec}$ ) of He-shell flash convection at a time just before the peak of He-flash
- Explicit, Eulerian, compressible grid code RAGE
- Initial conditions: piecewise polytropic stratification with gravity that closely resembles the actual conditions in a specific  $2M_{\odot}$ ,  $Z=0.01$  thermal pulse model



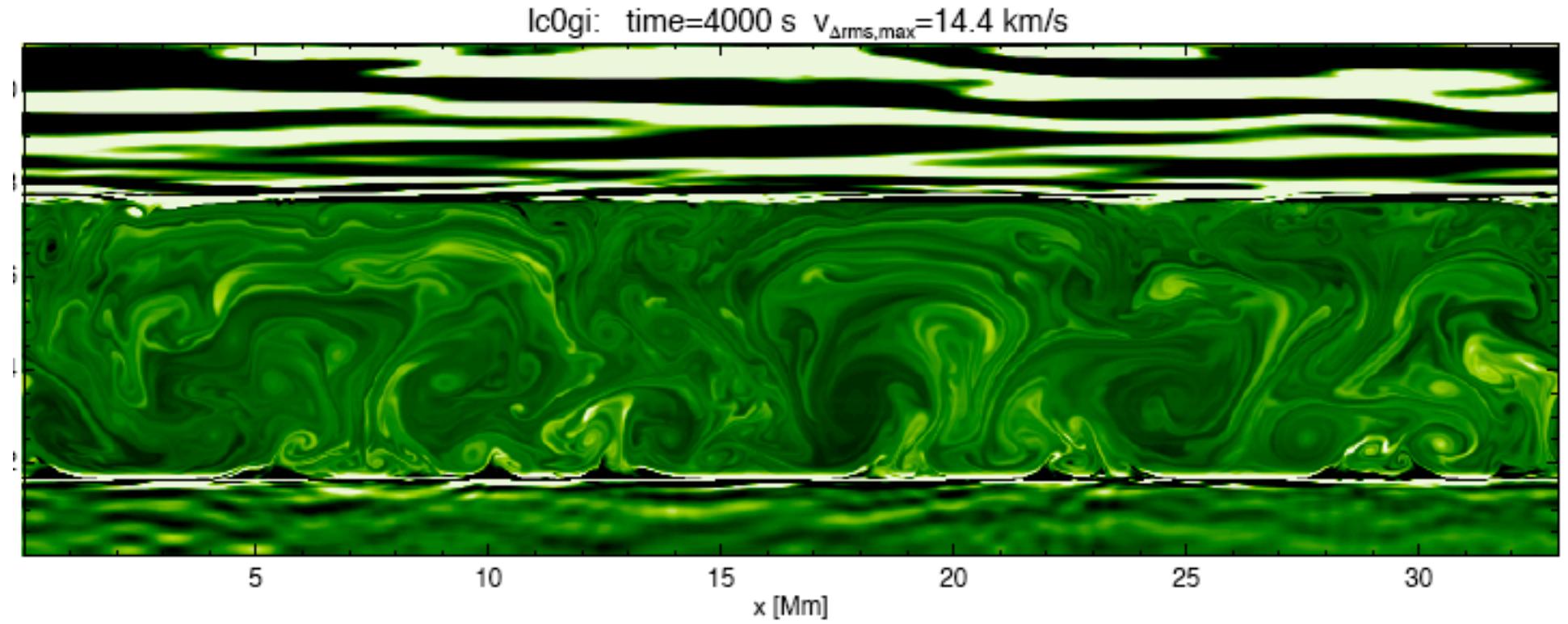
# Flow pattern

Ic0gh: time=4300 s  $v_{\Delta \text{rms}, \text{max}} = 16.2 \text{ km/s}$



Pressure fluctuations with pseudo-streamlines overplotted, 2D,  
1200x400, enhanced heating (30x) (Ic0gh)

## High-resolution run



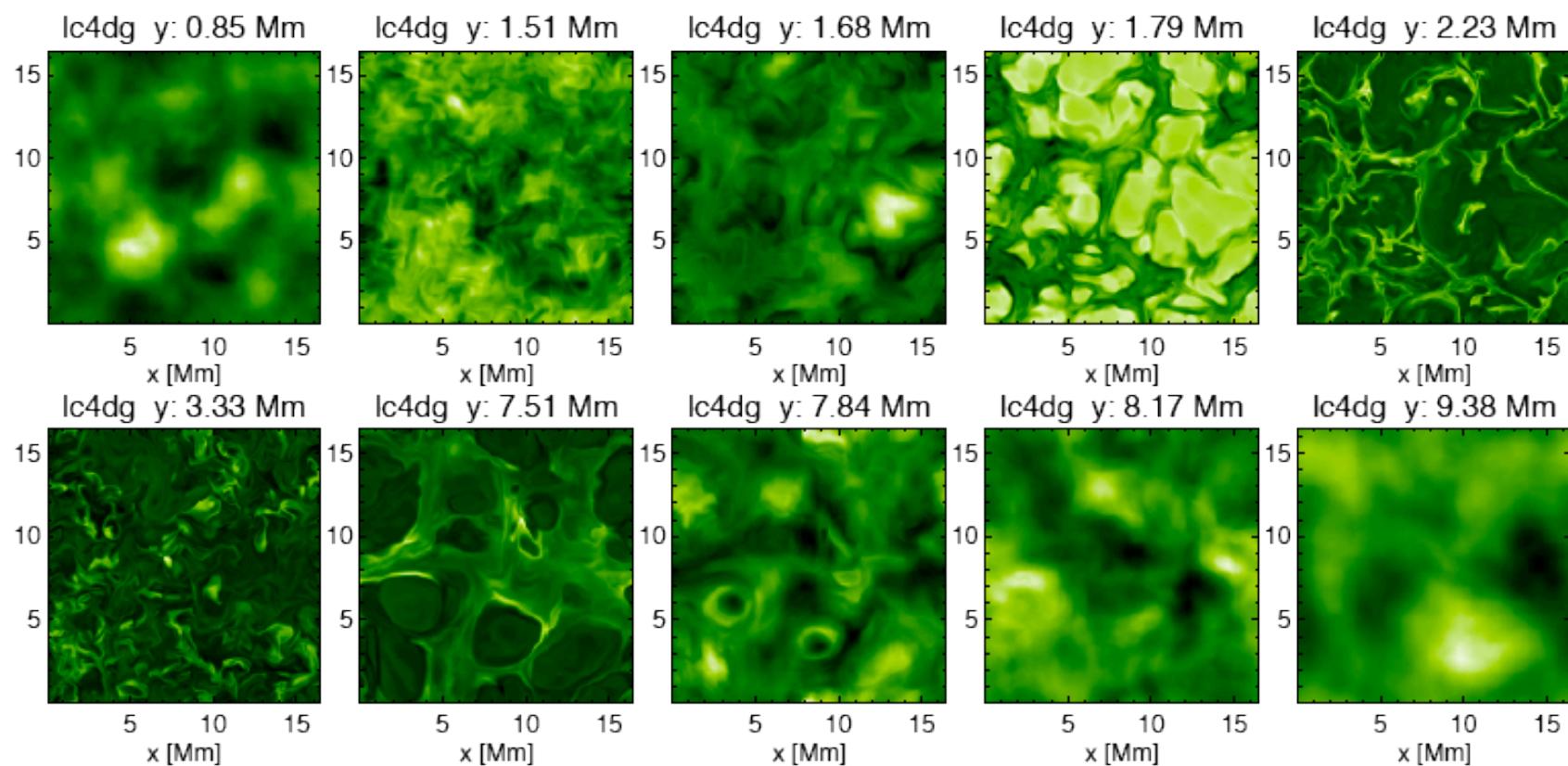
2D entropy fluctuations (2400x800), realistic heating rate  
Courant time scale at this resolution:  $\sim 3 \times 10^{-3} \text{ sec} \rightarrow 1.6 \text{ M cycles}$

# Movie 2D

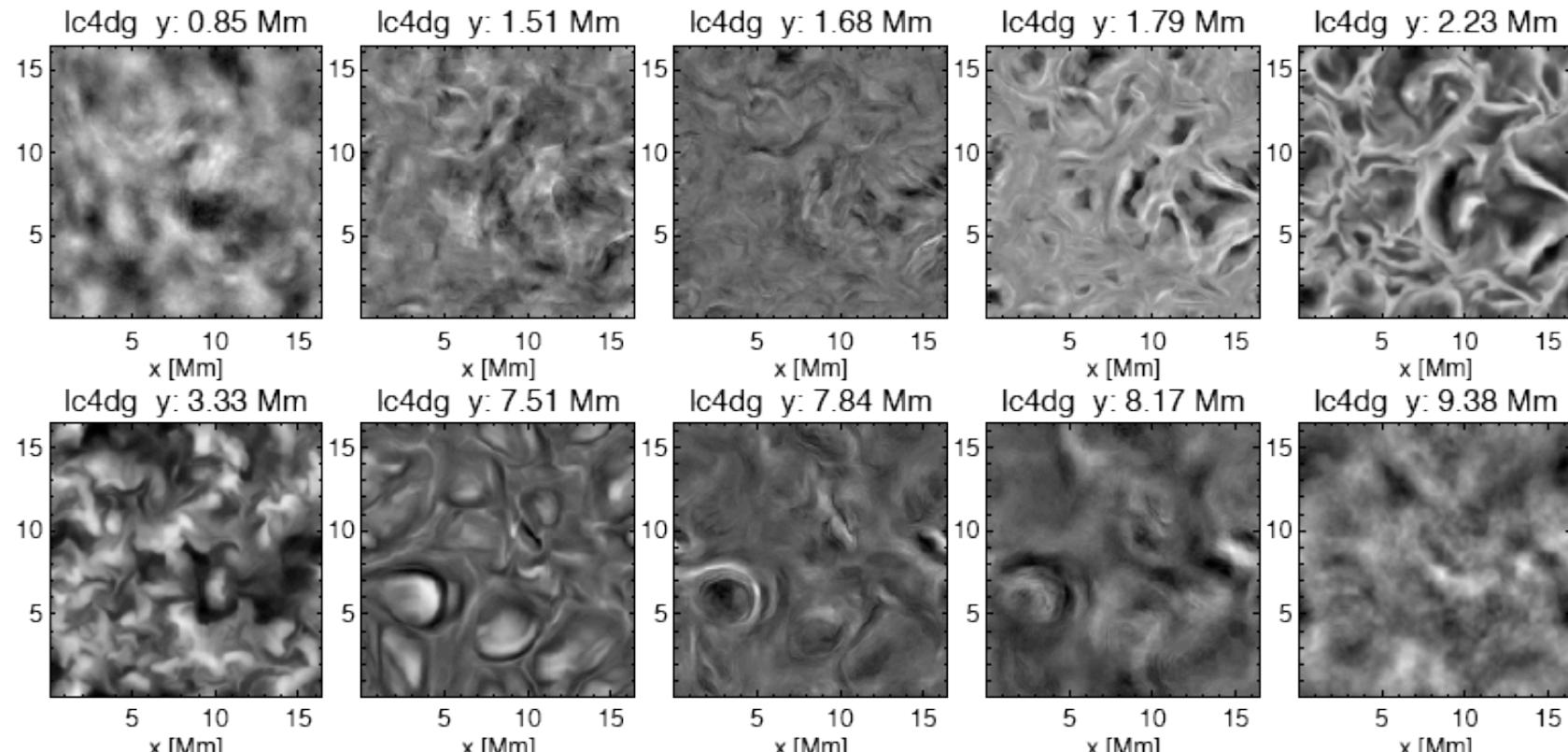
Insert here movie lc0gh.ds.mpg.

Entropy fluctuations, 2D, 1200x400, realistic heating (lc0gh)

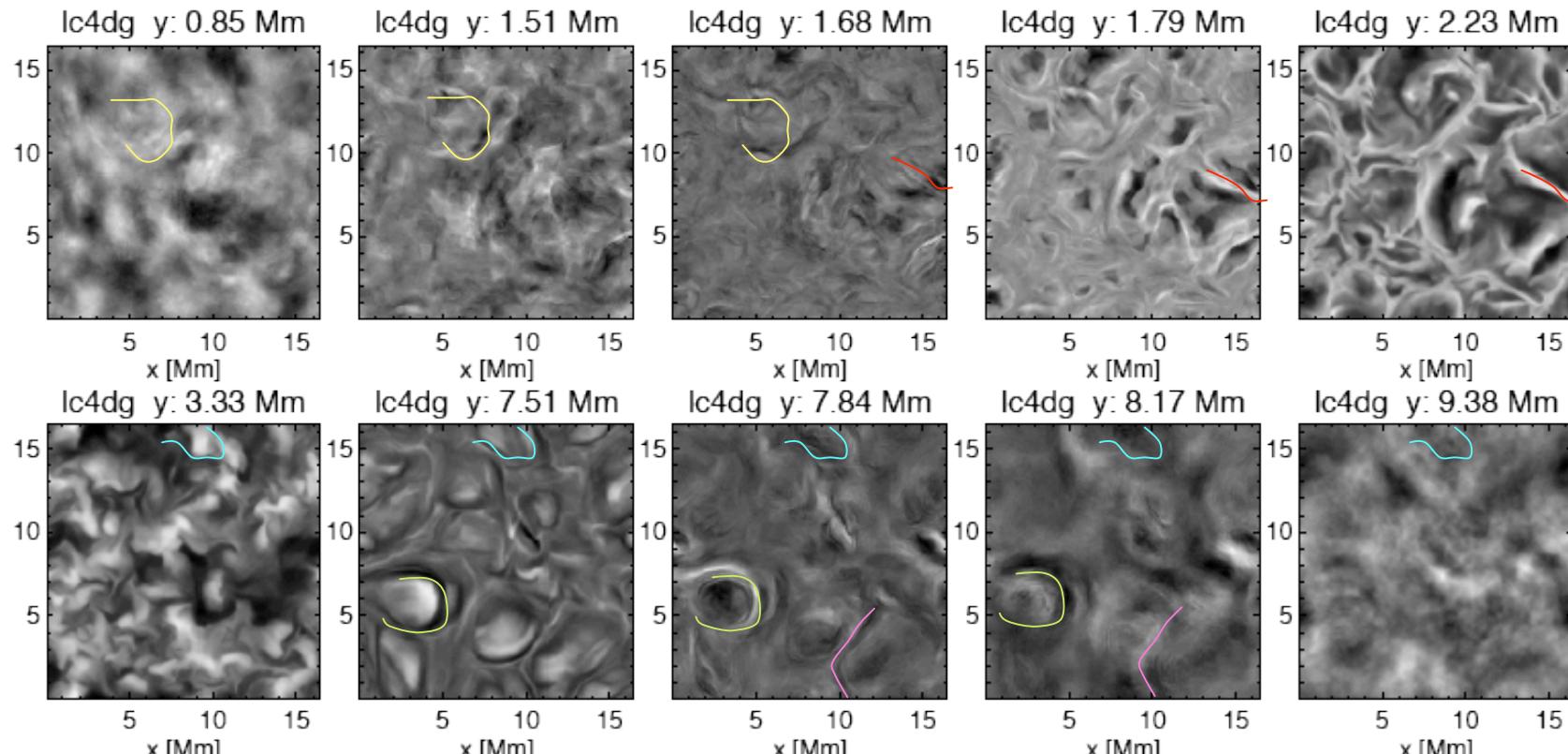
3-dimensional simulation:  $300^2 \times 200$ , enhanced heating (lc4dg)  
Horizontal slices of entropy fluctuations



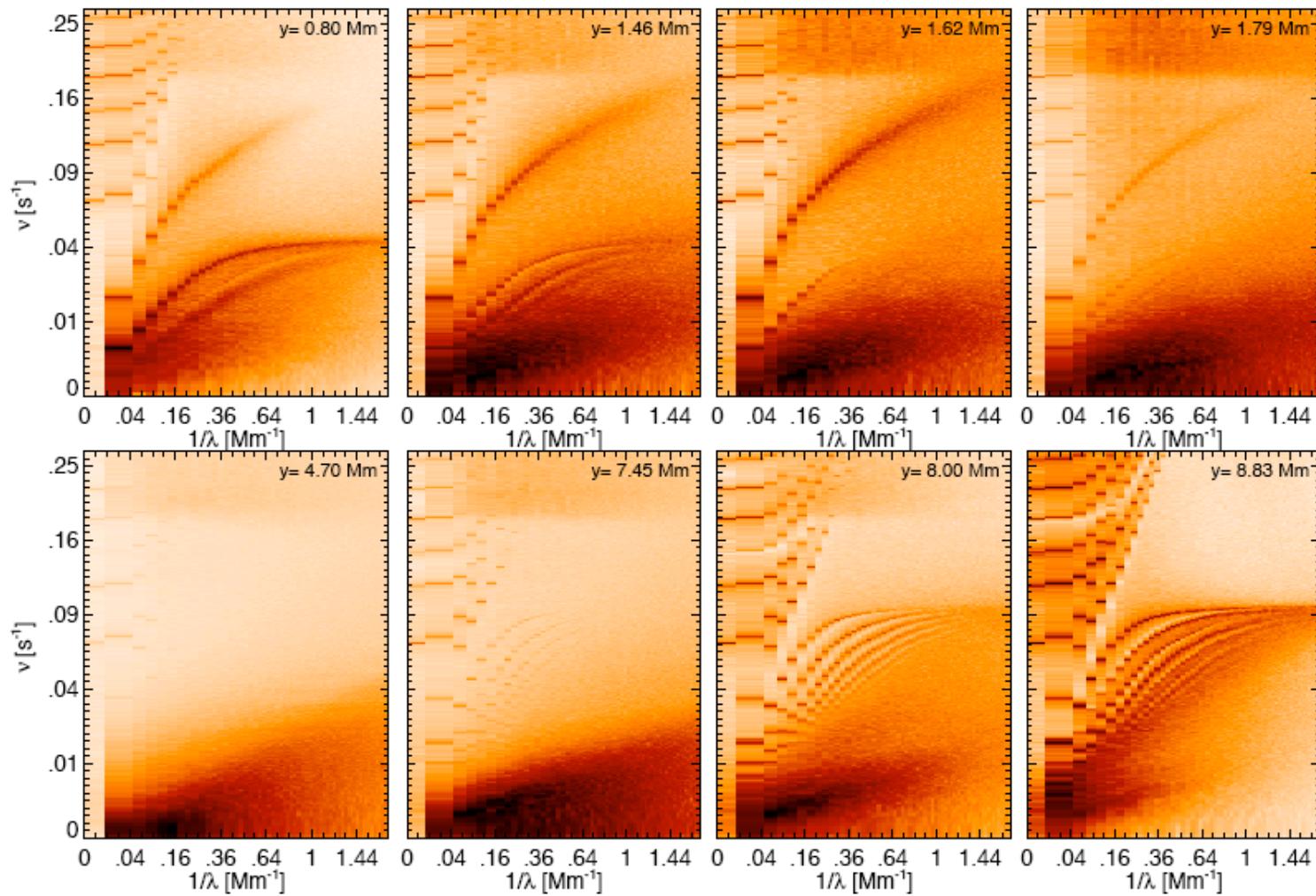
3-dimensional simulation:  $300^2 \times 200$ , enhanced heating (lc4dg)  
Horizontal slices of vertical velocity



3-dimensional simulation:  $300^2 \times 200$ , enhanced heating (lc4dg)  
Horizontal slices of vertical velocity

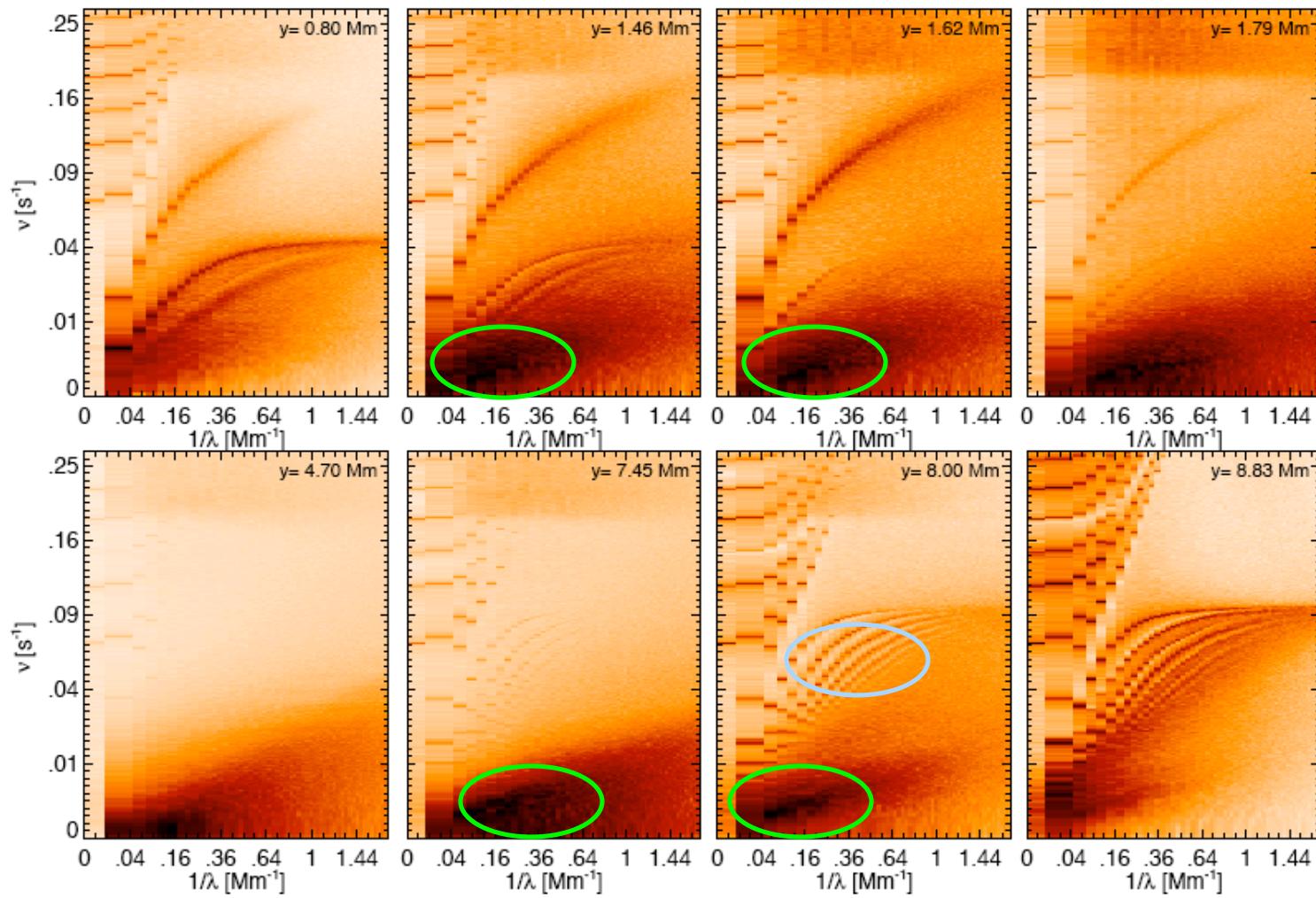


# Oscillation analysis



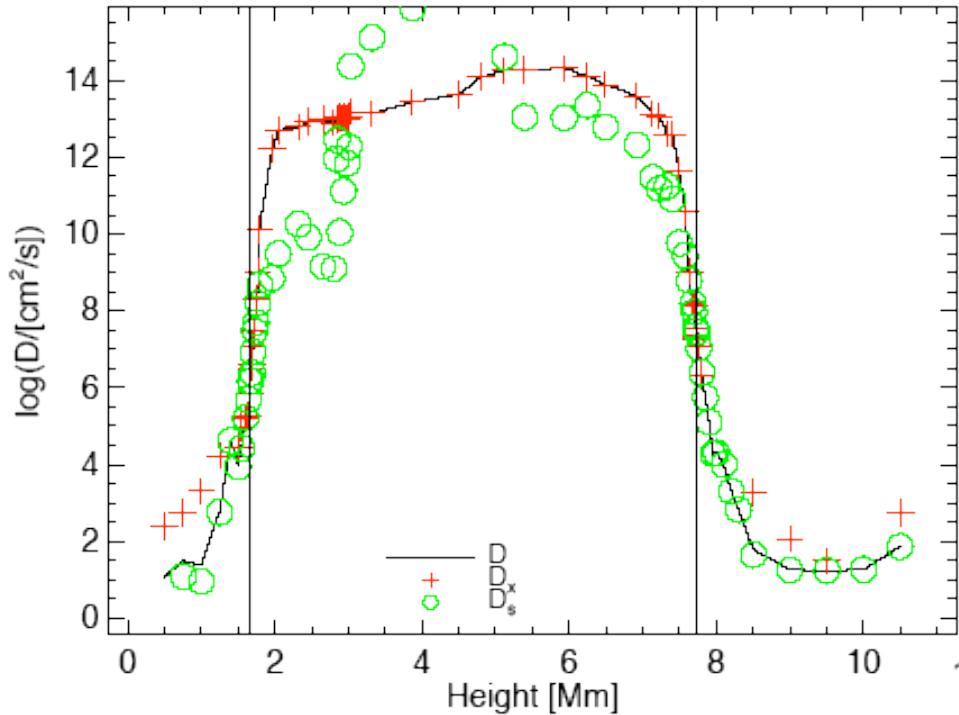
k- $\omega$  diagrams for various heights of benchmark run lc0gg

# Oscillation analysis



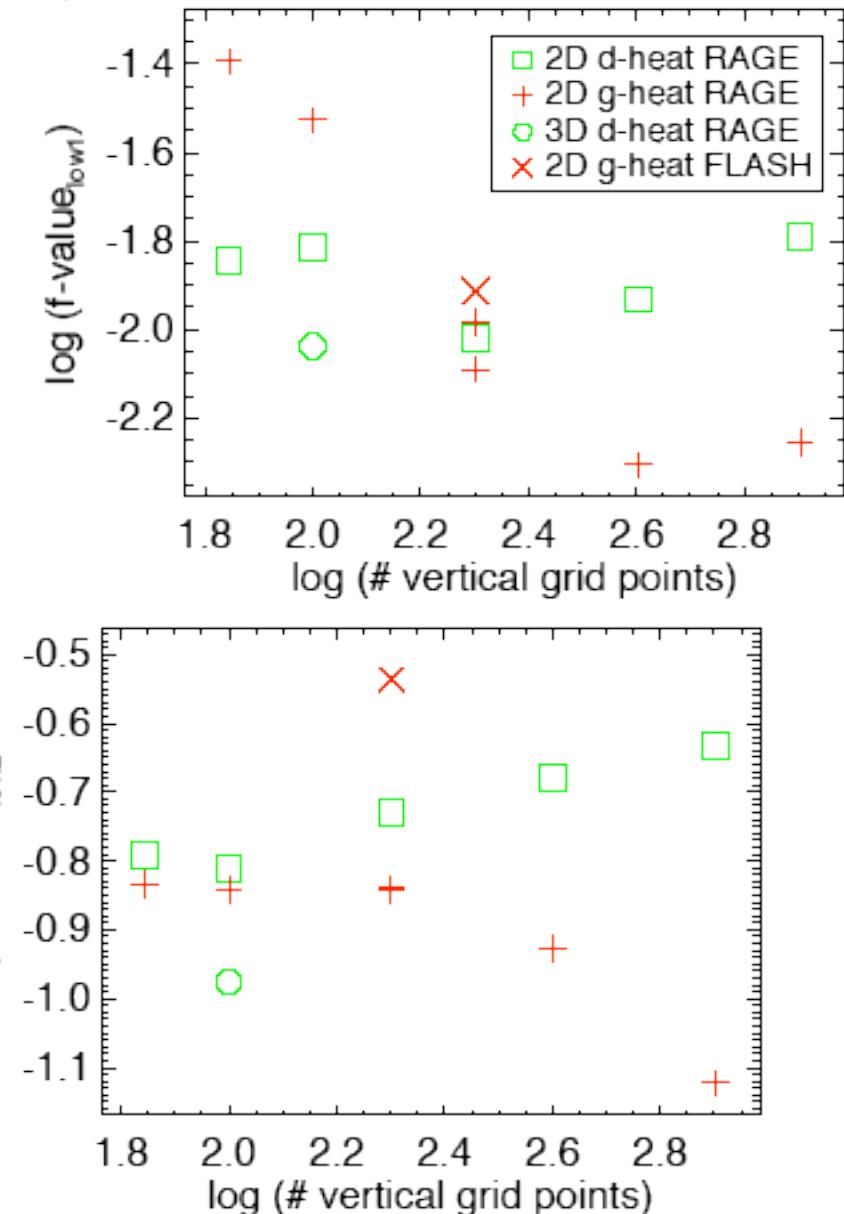
k- $\omega$  diagrams for various heights of benchmark run lc0gg

# Mixing of He-shell Flash Convection



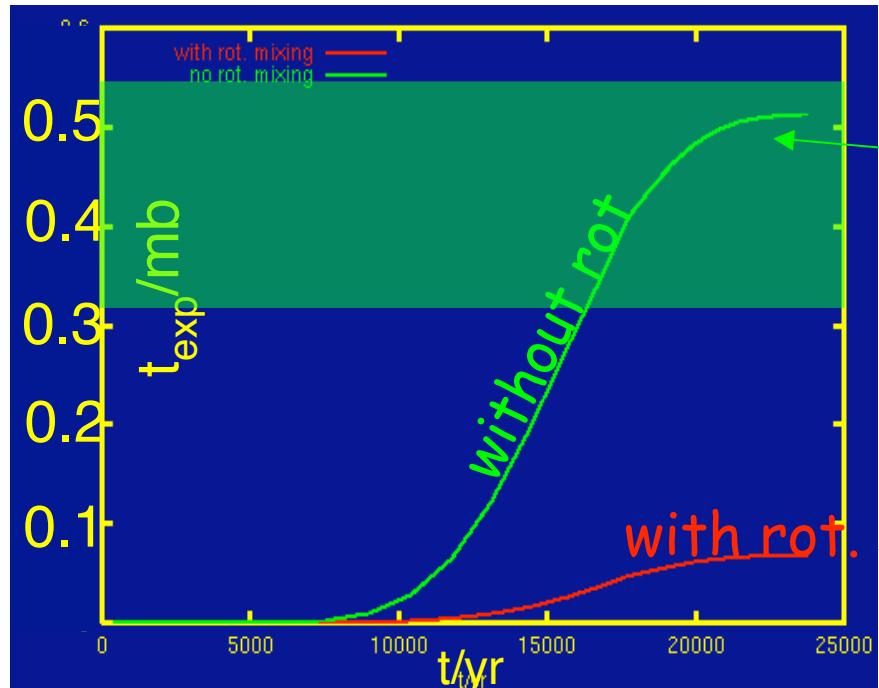
Diffusion coefficient reflecting hydrodynamic mixing (Freytag & Herwig, 2006, in prep.).

$$\begin{aligned} f_{\text{top}} &\sim 0.10 \\ f_{\text{bot},1} &\sim 0.01 \\ f_{\text{bot},2} &\sim 0.14 \end{aligned}$$



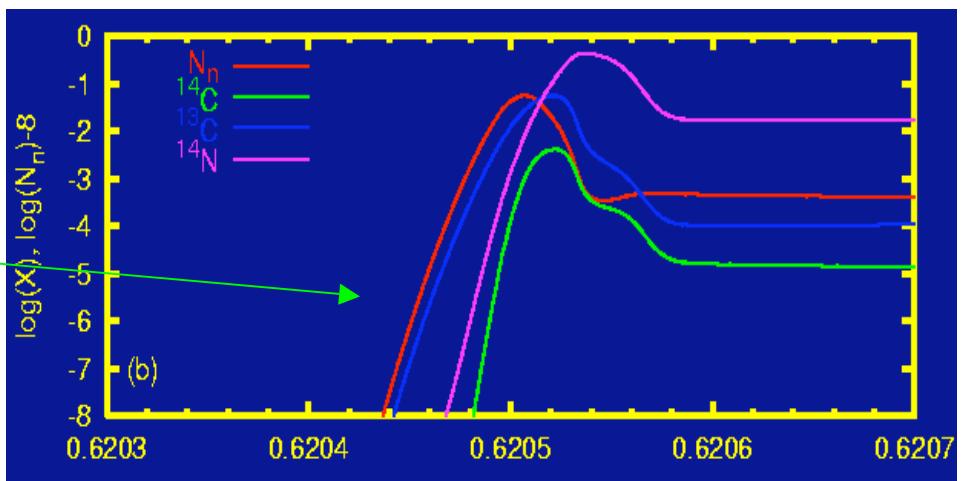
# s-process in rotating AGB Stars

Neutron exposure in s-process production site:

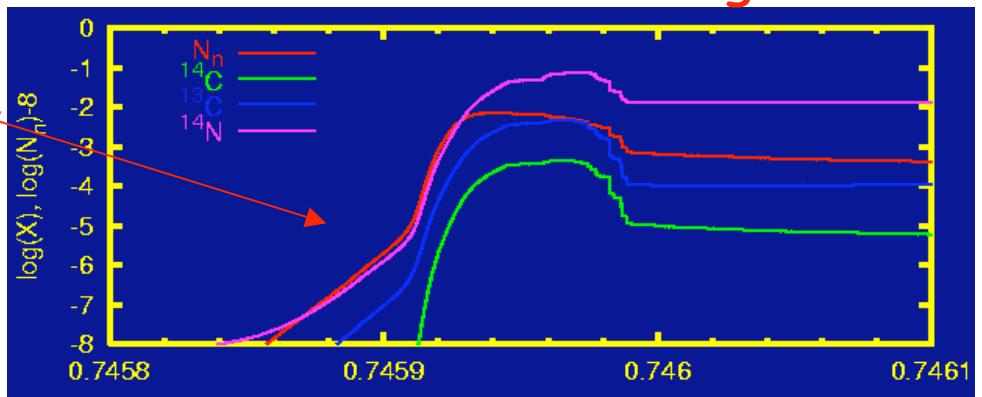


Herwig et al (2003), Siess et al. (2004)

overshoot mix, no rot mix

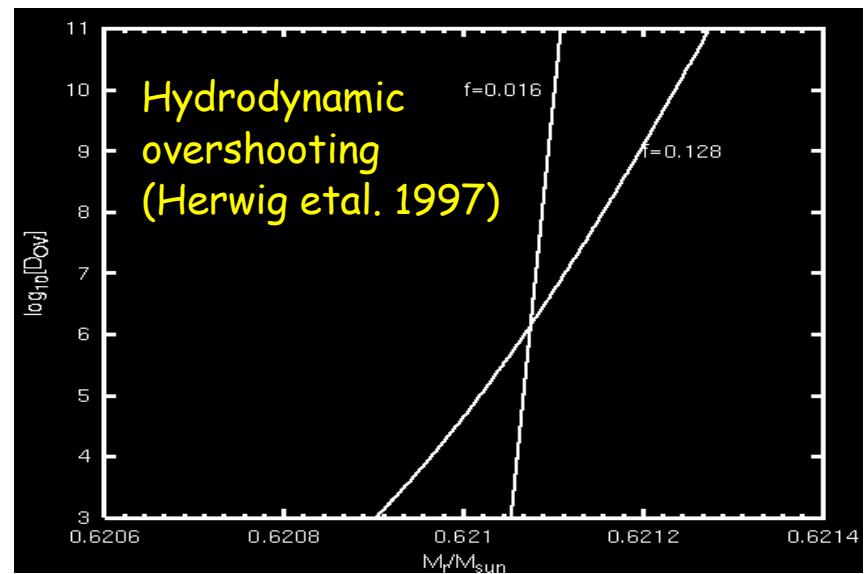
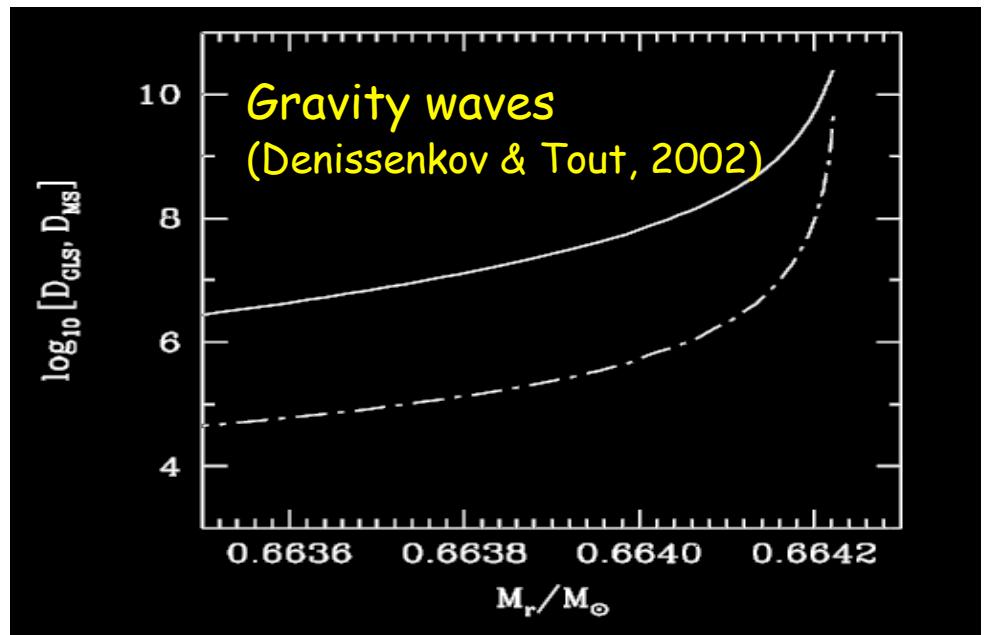
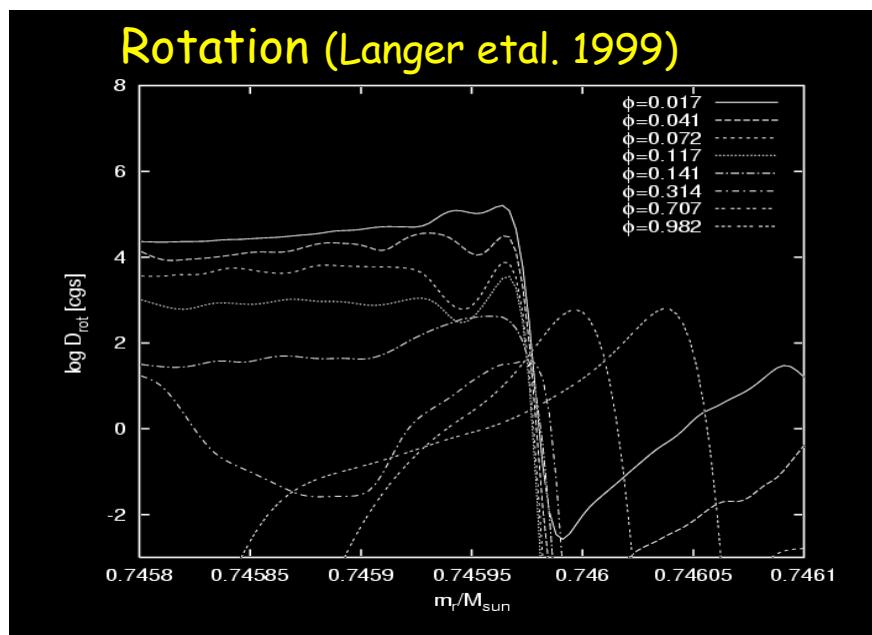


with rot mixing

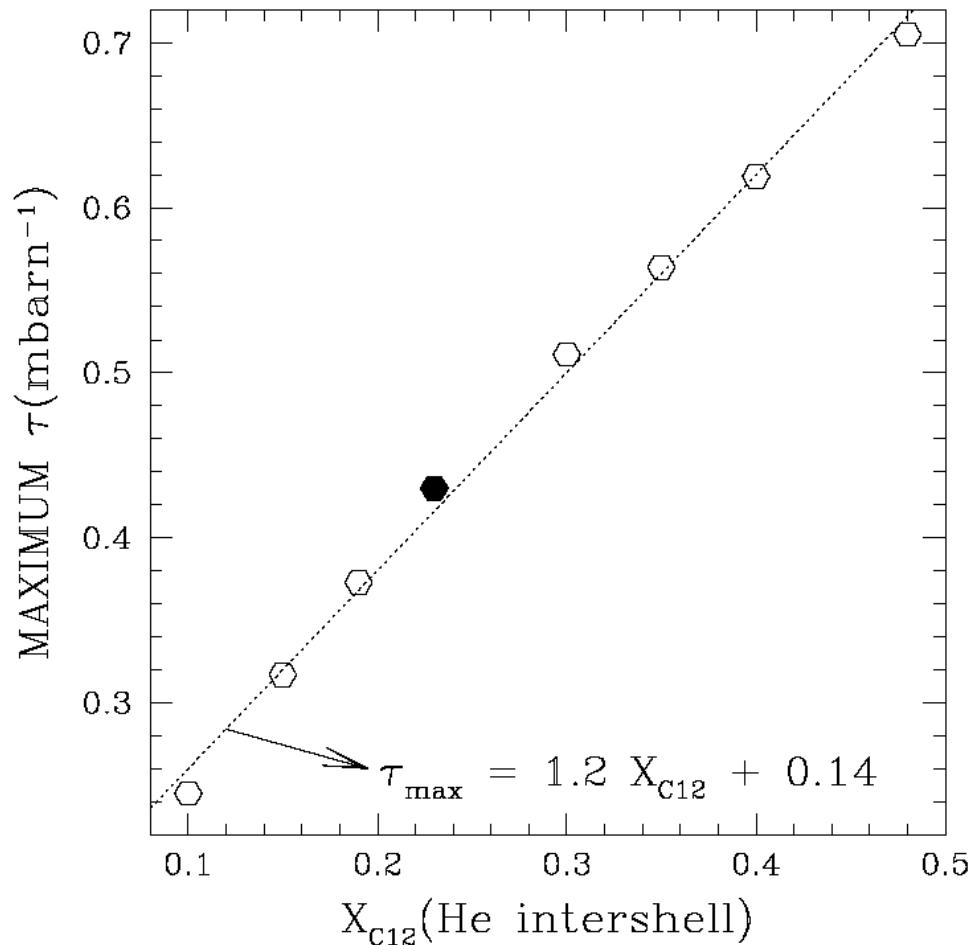


## Mixing for the $^{13}\text{C}$ pocket

Mixing processes for the radiative s-process (partial mixing of protons with  $^{12}\text{C}$  at the base of the convective envelope during/after 3DUP)



# Intershell C abundance vs. max neutron exposure in subsequent $^{13}\text{C}$ -pocket



Larger  $^{12}\text{C}$  intershell abundance results in larger  $^{13}\text{C}$  abundance in pocket, and thus larger max. neutron exposure.

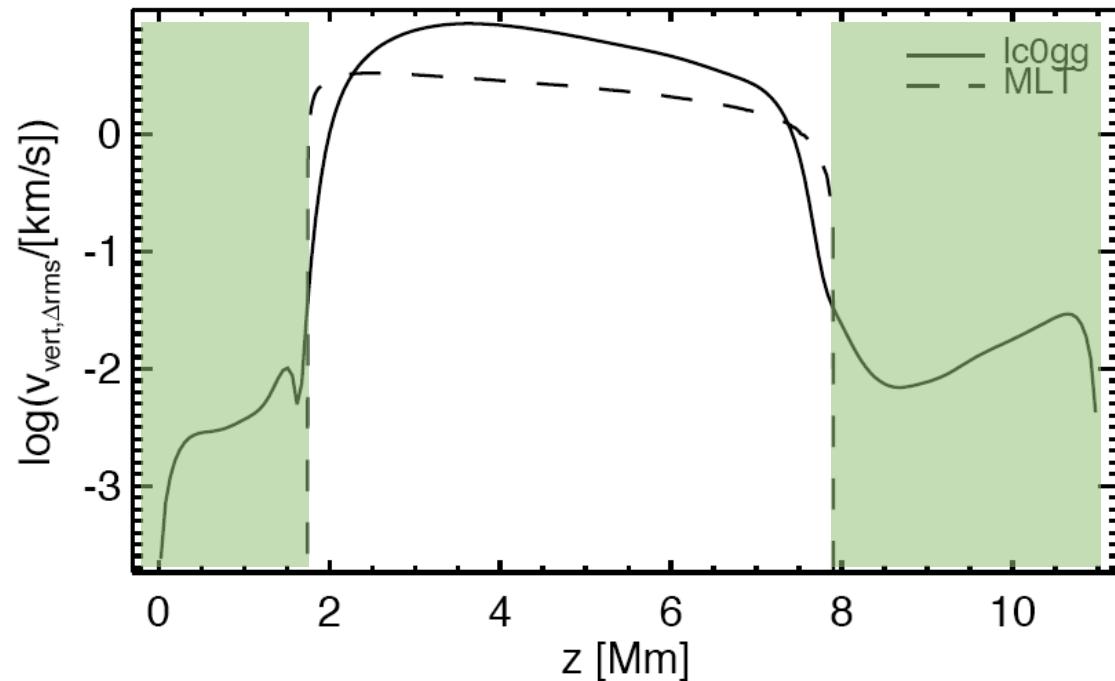
Lugaro et al. 2003

# Conclusions

- Full hydrodynamic simulations of convection in AGB stars, both in the envelope and in the intershell are now becoming feasible, and offer a new exciting tool to study mixing.
- Our simulations of He-shell flash convection allow a first quantitative glimpse at mixing at and across the convective boundary.
- The simulations emphasise the need to study the role of gravity waves in much greater detail.
- Rotating models do currently not reproduce observables.

After this slide: discussion slides.

# Comparison with MLT

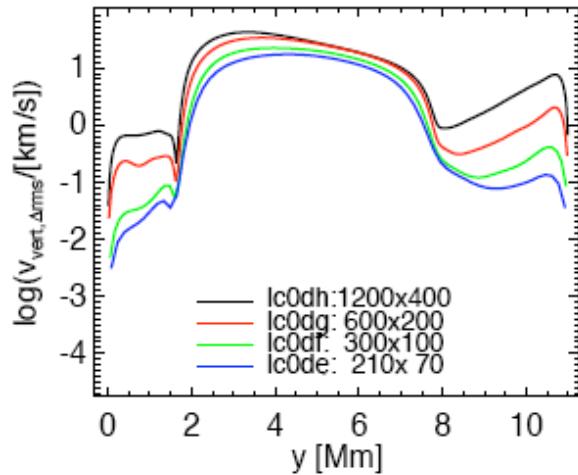


Comparison of rms-  
vertical velocities  
from hydro  
simulation Ic0gg and  
the mixing-length  
theory velocities  
from the 1D-stellar  
evolution model.

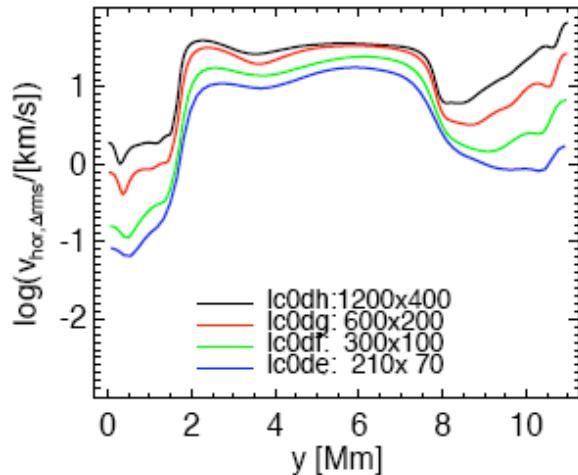
Velocities from internal gravity waves

# Convergence

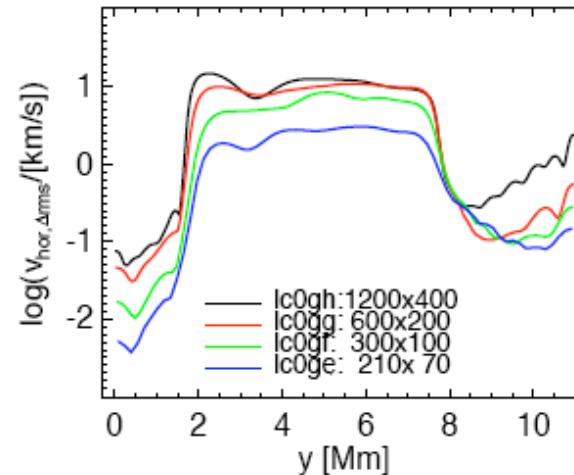
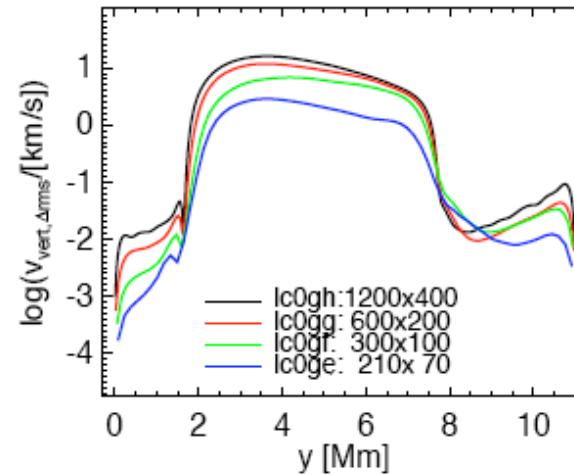
vertical v



horizontal v



Driving × 30



x1

# The grid

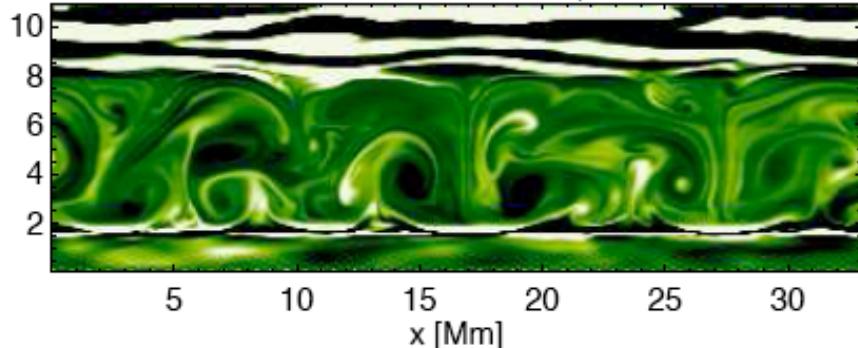
Resolution →

	e 210x70	f 300x100	g 600x200	h 1200x400	I 2400x800
c	100		10000		
d	30	10000	10000	10000	4600 900
e	10		10000		
f	3		10000		
g	1	10000	15000	16500	4300
h	1./3.		10000	16500	
I	1./10.		10000	20000	

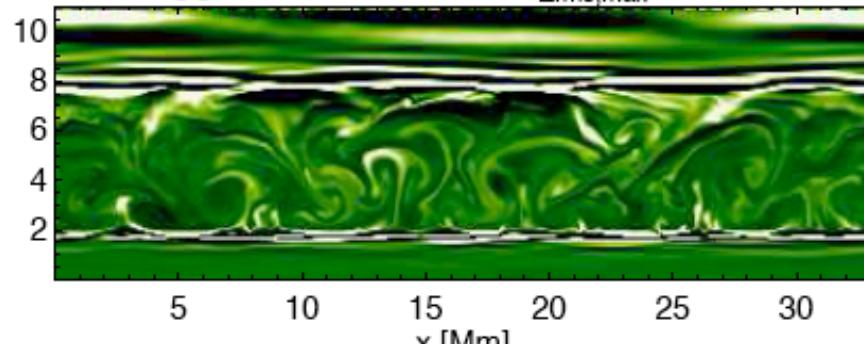
↑  
Energy  
driving

# Energy-driving sequence

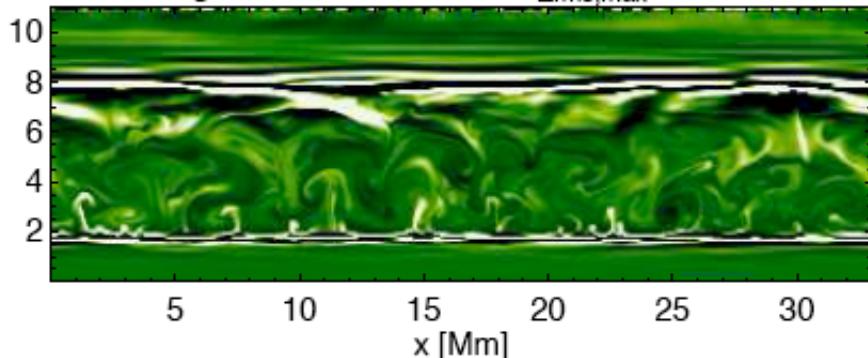
lc0cg: time=10000 s  $v_{\Delta \text{rms}, \text{max}} = 57.8 \text{ km/s}$



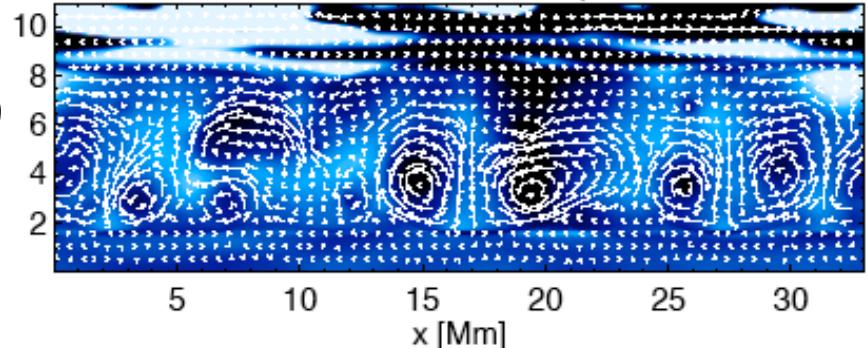
lc0gg: time=15000 s  $v_{\Delta \text{rms}, \text{max}} = 7.8 \text{ km/s}$



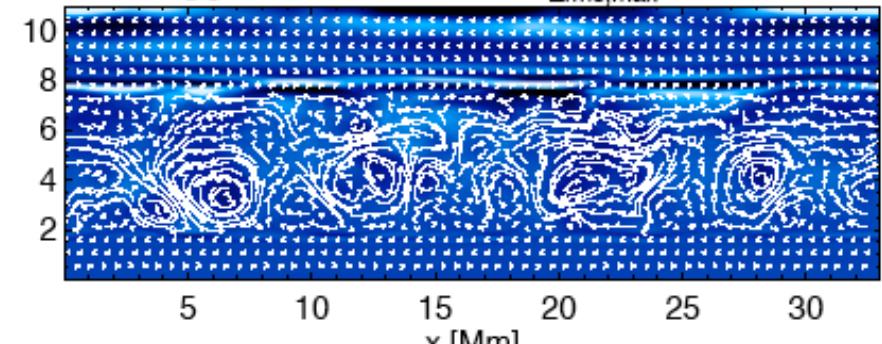
lc0hg: time=15000 s  $v_{\Delta \text{rms}, \text{max}} = 4.6 \text{ km/s}$



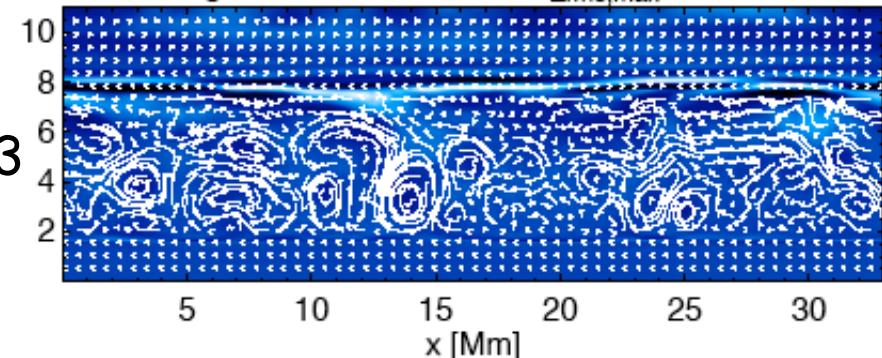
lc0cg: time=10000 s  $v_{\Delta \text{rms}, \text{max}} = 57.8 \text{ km/s}$



lc0gg: time=15000 s  $v_{\Delta \text{rms}, \text{max}} = 7.8 \text{ km/s}$

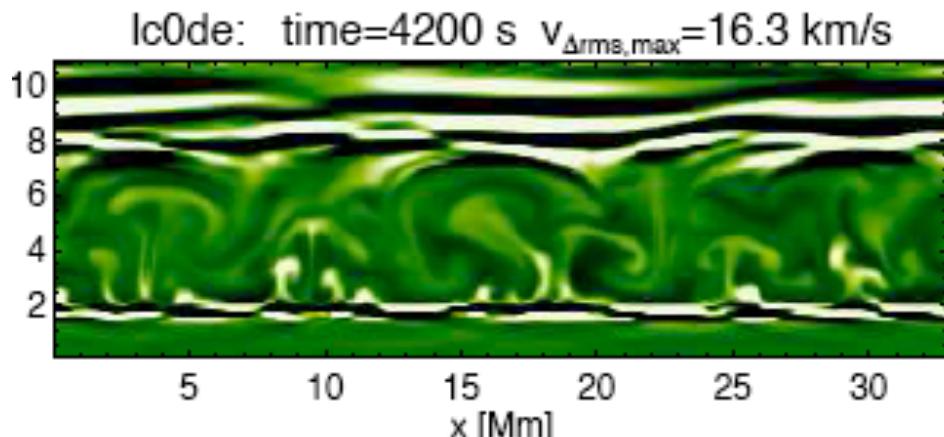


lc0hg: time=15000 s  $v_{\Delta \text{rms}, \text{max}} = 4.6 \text{ km/s}$

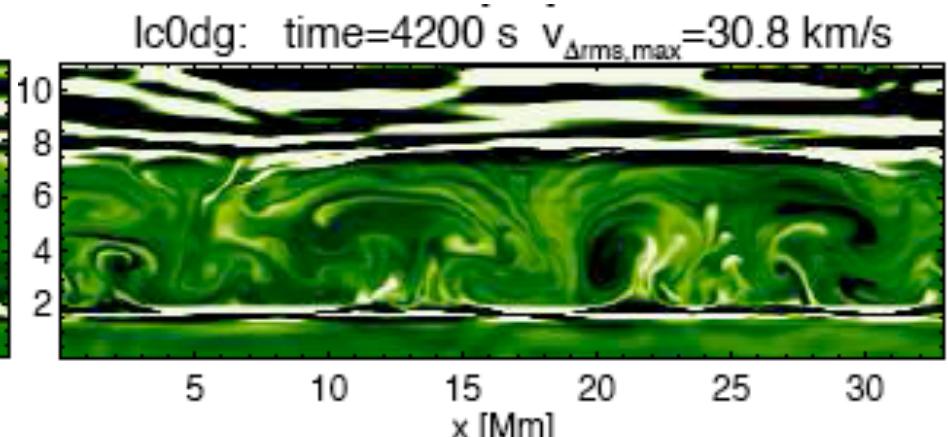


# Resolution sequence

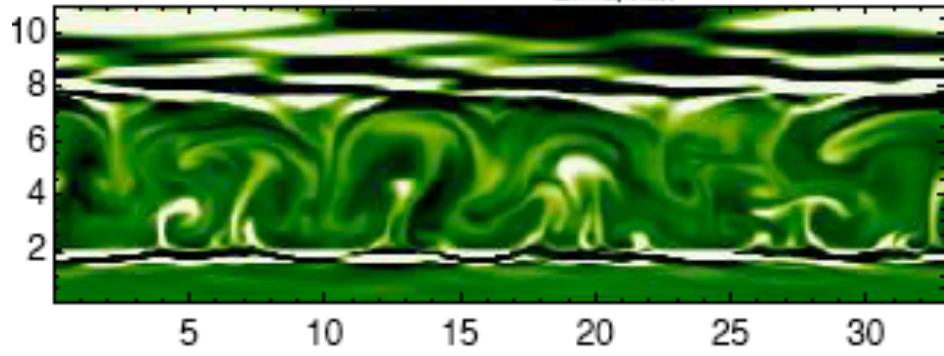
210x70



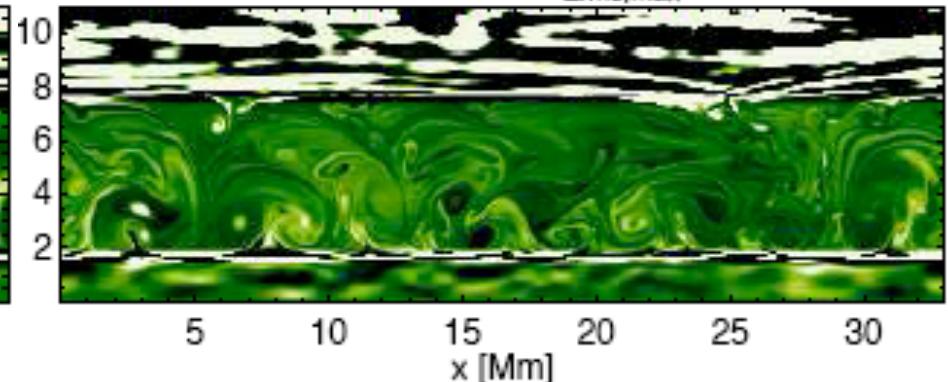
600x200



lc0df: time=4200 s  $v_{\Delta \text{rms}, \text{max}} = 25.8 \text{ km/s}$



lc0dh: time=4200 s  $v_{\Delta \text{rms}, \text{max}} = 41.0 \text{ km/s}$



300x100

1200x400

Energy driving x30